# **UNCLASSIFIED**

# AD NUMBER AD892612 **NEW LIMITATION CHANGE** TO Approved for public release, distribution unlimited **FROM** Distribution authorized to U.S. Gov't. agencies only; Test and Evaluation; Dec 1971. Other requests shall be referred to Air Force Armament Lab., Eglin AFB, FL 32542. **AUTHORITY** AFAL ltr, 24 Jun 1974

# AFATL-TR-71-169 VOLUME II



# CLOSE AIR SUPPORT MISSILE GUIDANCE AND CONTROL STUDY

**VOLUME II. THREE-DEGREE-OF-FREEDOM SIMULATION** 

DEPARTMENT OF MECHANICAL ENGINEERING
THE UNIVERSITY OF FLORIDA

TECHNICAL REPORT AFATL-TR-71-169, VOLUME Π

DECEMBER 1971

DDC PROFITE [ MAR 24 1972 ]

Distribution limited to U. S. Government agencies only;

December 1971. Other requests for this document must be referred to the Air Force Armament Laboratory (DLWG), Eglin Air Force Base, Florida 32542.

# AIR FORCE ARMAMENT LABORATORY

AIR FORCE SYSTEMS COMMAND . UNITED STATES AIR FORCE

EGLIN AIR FORCE BASE, FLORIDA

# Close Air Support Missile Guidance And Control Study

Volume II. Three-Degree-Of-Freedom Simulation

J. Mahig

TEST + EVALUATION

Distribution limited to U. S. Government agencies only; this report documents the close all support missiles is a control study, distribution limitation applied December 1971. Other requests for this document must be referred to the Air Force Armament Laboratory (DLWG), Eglin Air Force Base, Florida 52542.

#### **FOREWORD**

This report was prepared by the Industrial and Experiment Station, Department of Mechanical Engineering, University of Florida, Gainesville, Florida, under Contract No. F08635-71-C-0073 with the Air Force Armament Laboratory, Eglin Air Force Base, Florida, during the period from 9 December 1970 to 9 December 1971. Lieutenant Robert J. Karner (DLWG) monitored the project for the Armament Laboratory.

The principal investigator for the contractor was Dr. J. Mahig.

This report consists of two volumes. Volume I is devoted to the Six-Degree-of-Freedom Simulation while Volume II is concerned with the Three-Degree-of-Freedom Simulation. This is Volume II.

This technical report has been reviewed and is approved.

HEYWARD H. STRONG

Acting Chief, Air-to-Surface Glided Weapons Division

#### ABSTRACT

This report describes in detail a three-degree-of-freedom program which can be used to determine the trajectory and miss distance of a guided missile system. The options for the program are such as to permit variation of the aerodynamics, seeker, autopilot, actuator, and missile motor performance for the purpose of accurately simulating a given missile design and evaluating the effects of any changes in system parameters. Sufficient detail has been included in the text to minimize the effort needed to update or modify the program presented.

TEST + EUN/UNTION

Distribution limited to U. S. Government agencies only; this report documents the class air support missile and and control study; distribution limitation applied December 1971. Other requests for this document must be referred to the Air Force Armament Laboratory (DLWG), Eglin Air Force Ease, Florida 32542.

#### "PRECEDING PAGE BLANK-NOT FILMED".

# TABLE OF CONTENTS

Section	Title	Page
I	INTRODUCTION	1
II	STATE VARIABLES	3
III	SYSTEM EQUATIONS	5
3.1	Equations of Motion	5
3.2	Seeker Equations	9
3.3	Autopilot Equations	9
3.4	Nominal Thrust Profile	10
3.5	Current Input Configuration	10
3.6	Guidance Laws	10
IV	PROGRAM DESCRIPTION	11
4.1	Program Aids	11
Appendix		
I	PROGRAM LISTING	15
11	AERODYNAMIC CURVES	27
	REFERENCES	36

# LIST OF FIGURES

Figure	Title	Page
1.	Coordinate System	7
2.	Autopilot Block Diagram	9
3.	Input-Output Format	12
II-1.	Aero Pitch Damping Curve	28
11-2.	Aero Roll Damping Curve	29
11-3.	Center of Pressure Location	30
II-4.	Tail Misalignment Coefficient	31
11-5.	Body Normal Force	32
II-6.	Control Vane Normal Force	33
11-7.	Induced Drag	34
11-8.	Drag Force	35

# LIST OF TABLES

Table	Title	Page
I	Program Variable and State Variable Identification	4
11	Equivalence of Aerodynamic Coefficient Notation	6
III	Variable Listing	8
IV	Program Nomenclature	13

vii

(The reverse of this page is blank)

#### \*PORCEDING PAGE BLANK\_NOT FILMED\*.

#### SECTION I

#### INTRODUCTION

The purpose of the report is to describe in detail the equations used and the form required for the input data to a three-degree-of-freedom simulation of a laser guided missile system. The primary purpose of a three-degree-of-freedom simulation is to make possible the study of the characteristics of a given missile system quickly and economically. Since cross-coupling effects influence a missile's performance through the seeker, autopilot, and missile dynamics, any results obtained must be considered as preliminary until justified by a six-degree-of-freedom simulation.

Examples of some of the studies which can be usefully made are optimization of the seeker, autopilot gain, and noise sensitivity. The noise sensitivity studies include not only electronic noise but spot motion and signal loss simulation. Once the parameters for a given missile have been entered, it can be used efficiently even on a small computer since the program only requires 17,000 words of core.

The program for a specific missile is given in Appendix I. This program is made up of four parts: the main program and the subroutines DER, MODAMS, and GAUSS. The main program modifies input data to conform to program logic and maintains sole control for batch processing requirements. The subroutine DER retains control only over a given missile flight. The purpose of this routine is to determine the current value of the aerodynamic coefficients and angle of attack; provide limiters (e.g., fin deflection and electronic saturation); and determine the present value of the derivative of the state variables. The subroutine DER then updates the state variables by calling the subroutine MODAMS which integrates the entire system of equations using an Adams-Moulton predictor-corrector method with a Runge-Kutta start. The subroutine GAUSS is used by DER to generate a set of random variables which are used to determine the position of a laser spot and the apparent location of the target with respect to the missile. The routine is also used to determine pulse loss through the variable VLAZRP.

All the aerodynamic coefficients are either a function of Mach number or of the fin deflection. The aerodynamic coefficients used in this program are plotted in Appendix II. These plots are used to develop the aerodynamic coefficients as approximate functions of the dependent variable Mach number and fin deflection. The procedure makes DER compute much faster than would be possible through a table look-up procedure and need not detract from the accuracy.

#### SECTION II

#### STATE VARIABLES

A discussion of state variable techniques is given in many control theory books (1,2,3). However, a discussion of these techniques is appropriate at this point since they are used in the program to determine the missile's flight path.

The equation of motion governing pitch of the missile is given below in the familiar form:

$$\mathbf{I}_{\mathbf{y}\mathbf{y}}\ddot{\boldsymbol{\theta}} = \mathbf{M}_{2} \tag{1}$$

where M<sub>2</sub> is considered a function of time and the state variables. To convert this to state variable notation, the second order equation must first be converted into two first order equations. (This is also true for an nth order system which, in order to be converted into the state variable form, must first be converted into n' order systems.) Equation (1) is converted through owing definitions:

$$\dot{\theta} \equiv \theta_2$$

$$\dot{\theta}_2 \equiv M_2$$

Now, since  $\text{M}_2$  is a function of  $\theta$  and  $\theta$  and t, then the system may be defined in state variable form as

$$\dot{\theta} = \theta_2$$

$$\dot{\theta}_2 = M_2(\theta, \theta_2, t).$$

This same process can be used for an nth order system.

A list of the state variables and their derivatives in DER is given in Table I.

TABLE I. IROGRAM VARIABLE AND STATE VARIABLE IDENTIFICATION

	State Variable	State Variable Derivative
1.	x - Y(1,1)	$\dot{x} - YP(1,1)$
2.	x - Y(2,1)	$\ddot{X} - YP(2,1)$
3.	Z - Y(3,1)	Ż - YP(3,1)
4.	ż - Y(4,1)	$\ddot{2} - YP(4,1)$
5.	λ <sub>S</sub> - Y(5,1)	$\dot{\lambda}_{S} - YP(5,1)$
6.	λ - Υ(6,1)	λ - YP(6,1)
7.	δ - Y(7,1)	$\delta - YP(7,1)$
8.	δ - Υ(8,1)	ö - ΥΡ(8,1)
9.	ő - Υ(9,1)	$\delta - YP(9,1)$
10.	θ - Υ(10,1)	$\dot{\theta} - YP(10,1)$
11.	ė - Y(11,1)	ë - YP(11,1)
12.	R - Y(12,1)	Ř - YP(12,1)
13.	φ - Y(13,1)	$\dot{\phi} - YP(13,1)$
14.	φ <sub>M</sub> - Y(14,1)	φ <sub>M</sub> - YP(14,1)

Note: State Variables  $R,\phi,\phi_M$  are the results of proportional guidance implementation. The implementation is assumed ideal.

#### SECTION III

#### SYSTEM EQUATIONS

## 3.1 Equations of Motion

The equations of motion for the three-degree-of-freedom simulation used in the program are developed as follows:

The forces in body axes -

$$F_{1} = -(C_{A} + 2C_{A\delta} | \delta |) qs + TH$$

$$F_{3} = -(C_{N\alpha} \alpha + C_{N\delta} \delta) qS$$

$$M_{2} = (-C_{N\alpha} (X_{CP} - X_{CG}) \alpha + C_{N\delta} (X_{CG} - X_{C}) \delta) qsd$$

$$-C_{MA} \theta (\rho V_{A}/4) sd^{2}$$

Table II defines the relationship between the commonly used aerodynamic coefficients, used above, with the variable names used in the fortran program listing shown in Appendix I.

The equations of motion in the earth fixed coordinate system are:

$$m\ddot{X} = F_1 \cos\theta + F_3 \sin\theta$$
  
 $m\ddot{Z} = -F_1 \sin\theta + F_3 \cos\theta + mg$   
 $I_{YY}\dot{\theta} = M_2$ 

where the quantities  $\alpha$ ,  $V_A$ , and q are defined as follows:

$$\alpha = V_{ZA}/V_{XA} \qquad (\alpha < 15^{\circ})$$

$$V_{A} = \sqrt{V_{XA}^{2} + V_{ZA}^{2}}$$

$$q = \frac{1}{2}\rho V_{A}^{2}$$

and the variables  $V_{\rm XA}$  and  $V_{\rm ZA}$  (the velocity along and perpendicular to the missile centerline) are given as:

$$V_{XA} = \dot{X} \cos \theta - \dot{Z} \sin \theta$$
  
 $V_{ZA} = \dot{X} \sin \theta + \dot{Z} \cos \theta$ 

TABLE II. EQUIVALENCE OF AERODYNAMIC COEFFICIENT NOTATION

Aerodynamic Coefficient	Program Variable
C <sub>A</sub>	CA
C <sub>A</sub> 6	DCA
c <sub>N</sub> a	CNA
c <sub>N δ</sub>	CND
c <sub>M</sub> ė	СМТ
c <sub>M</sub> <sub>δ</sub>	CMD

Figure 1 and Table III respectively, contain the coordinate system used in the derivation of the equations of motion presented above and define those other terms used as necessary.

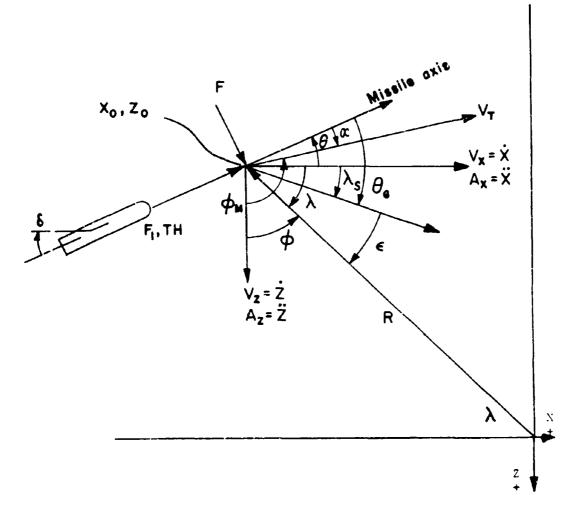


Figure 1. Coordinate System

#### TABLE III. VARIABLE LISTING

- X Position of missile in X direction
- Z Position of missile in Z direction
- $\lambda_{S}$  Line of sight of seeker
  - $\lambda$  Line of sight of missile
  - ← Fin Deflection
  - $\theta$  Pitch of missile
- $t_{\alpha}$  Guidance delay
- m Mass of the missile
- $I_{VV}$  Moment of inertia
- q Dynamic pressure
  - S Reference area
  - d Diameter of missile
  - ρ Density of sir (slugs per cubic feet)
- TH Thrust force
  - g Gravity
- $V_{\chi_{\lambda}}$  Velocity along missile axis
- $V_{\mathrm{ZA}}$  Velocity perpendicular to missile axis
- V<sub>A</sub> Total velocity of the missile
  - $\alpha$  Angle of attack of the missile
- $\mathbf{X}_{\text{cp}}$  Location of center of pressure (calibers)
  - X<sub>c</sub> Location of fin (calibers)

# 3.2 Seeker Equations

The position of the target is always assumed to be at the location of the origin of the coordinate system. Thus, the line of sight may be given as

$$\lambda = \tan^1(2/X).$$

If the seeker is assumed to be a PLG seeker, then the variation of the seeker axis in terms of the missile orientation may be given as

$$\lambda_S = -\theta (1 + \tau_S S)$$
.

The angle between the line of sight and the seeker axis may be given as

$$\varepsilon = \lambda - \lambda_{S}$$
.

# 3.3 Autopilot Equations

The block diagram for the autopilot used in the program is given below in Figure 2.

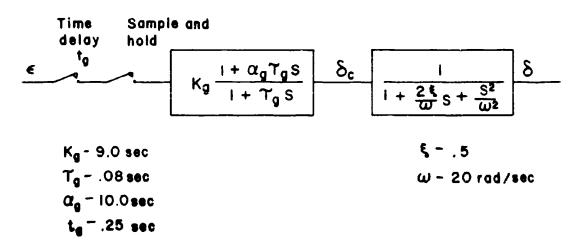


Figure 2. Autopilot Block Diagram

# 3.4 Nominal Thrust Profile

The initial thrust is

7500 lb; 0 < t < 0.8 seconds

which then linearly decreases to zero at 1.3 seconds.

# 3.5 Current Input Configuration

The input data for the missile configuration used is:

d = 0.416

S = 0.136

 $X_{cq} = 10.6$  (initial)\* [8.75 at burnout]

 $X_C = 8.4$ 

M = 4.21 (initial)\* [3.48 at burnout]

 $I_{yy} = 29.56$  (initial) [25.04 at burnout]

 $\tau_S \approx 5.0$ .

#### 3.6 Guidance Laws

Any guidance law may be simulated by the program; however, for convenience, some guidance implementations are prepackaged into the program. Thus, at the beginning of the subroutine DER is a list of commented cards containing the following statements:

- (a) Pursuit Guidance
- (b) PLG Guidance
- (c) Sidewinder Guidance (PNG).

These statements head the required changes in the program needed to implement that form of guidance. Thus, for example, implementation of PLG guidance only requires the replacement of the current calculation of YP(5,1) by the one following the card with the statement PLG GUIDANCE.

<sup>\*</sup>Variation in X<sub>Cg</sub> and M during motor burn is assumed proportional to the ratio of the impulse imparted to the total impulse available from the motor.

#### SECTION IV

#### PROGRAM DESCRIPTION

#### 4.1 Program Aids

In order to effectively coordiante the variables used in the program with the system equations developed above, Table I is to be used for the identification of the state variables and Table IV will provide definitions for the other variables used by the program. In addition, Figure 3 defines the form in which the input must be prepared and the output format of the program.

A complete listing of the program and its output is given in Appendix I. Appendix II contains the aerodynamic curves for an actual missile. These aerodynamic coefficients are all given as a function of Mach number. Since accurate functional representation of some of these curves are very complex, simple mathematical expressions were chosen which are true only over defined Mach number regimes. The adequacy of the representation may be assessed by the reader by comparing the results obtained from the equations listed in the program with the aerodynamic curves they are intended to represent. These curves are shown in Figure II-1 through Figure II-8.

## Input Format

## FORMAT (1P6E12.4)

FPT,H,TEN,AR,DVI,VI,DTH,ALP,RANGE,LOS,GBIAS,VLAZRP,XLASR,DSPEED,TZ

Y(13,1), Y(14,1)

#### Output Format

#### FORMAT (1P9E12.4)

Y(1,1), YP(1,1), Y(2,1), YP(2,1)... (5,1)

 $YP(5,1), Y(6,1) \dots YP(9,1)$ 

YP (14,1)

X,TACC

Figure 3. Input - Output Format.

TABLE IV. PROGRAM NOMENCLATURE

н	Time increment, DT
TEN	Angular orientation of thrust vector
AR	Offset of rocket motor from center line of missile
DVI	Change in missile velocity in feet/second (initial condition)
VI	Initial velocity of missile
DTH	<pre>Increment in the line of sight   (for next run)</pre>
ALP	Angle of attack (in degrees)
RANGE	Range of target along line of sight (feet)
Los	Line of sight, angle in degrees (always positive)
GBIAS	Gravity bias term
FPT	Number of time increments not to be exceeded
x	Current time, initial time
MIT	Time of next laser pulse
THF	Thrust factor (not implemented)
MAC	Mach No.
ES	Surface area
ХСР	Location of c.g. in missile diameters
а	Missile diameter
TACC	Total acceleration magnitude
AL	Angle of attack a

TABLE IV. (CONCLUDED)

IXX	Moment of inertia in X direction
IYY	Moment of inertia in Y direction
IZZ	Moment of inertia in 2 direction
CA	Drag coefficient
DCA	Induced drag
CND	Control vane normal force
CNA	Body normal force
CMD	Tail misalignment coefficient
XCP	CP location - diameters from nose
CMT	Pitch damping coefficient
IC	Total number of increments of initial condition DTH
IK	Printout occurs every IK <sup>th</sup> increment of H
N	Number of state variables
XLASR	Standard deviation of laser spot in X direction
VLA2RP	Percent of time laser pulse acquired by seeker/100 (used in pulse loss logic)
TZ	Length of time for which seeker is caged (pursuit guidance)
TACC	Total accleration of missile
DSPEED	Counter (if greater than one, aircraft speed is incremented by DVl for next launch
DTH	Increment by which initial orientation is changed for next launch

APPENT X I
PROGRAM LISTING

```
EP=0.
     CCFFCR/VAR/TEN, AR, TIM, THF, TTK, TACC, GBIAS
    .,YFL,VLAZRP,XLASR
    .EP.FS.ER.TZ
     DIMENSICNY(14,6), YP(14,6), V(14)
     EXTERNALCER
     REALLOS
  1 CCNTINUE
     X≖Q.
     TIF40.
     IC = 10
     [ T = 0
     IK≠8
     N=14
      REAC(5,900) FPT, P, TEN, AR, DV1, V1, DTH, ALP, RANGE, LOS, GBEAS
    . VLAZRP. XLASR
    . CSPEEC.TZ
         HRITE(6,900) FPT, H, TEN, AR, DV1, V1, OTH, ALP, RANGE, LOS, GBIAS
    ., VLAZRP, XLASR
    . DSPEED.TZ
900 FCRMAT(1P6E12.4)
     MPT=FPT
     CTH=CTH/57.6
     DC41=1,14
     Y(1,1)=0.
     Y(12,1)=10001
     BBC=IC/2.CTH
    CONTINUE
     V1=V1+CV1
     PV=LCS/57.6
     Y(1,1) =-RANGE+CC9(PV)
     Y(3,1) = -RANGE+SIN(PV)
     Y (6, L) = PV
     Y(5,1)=Y(6,1)
     Y(10,1) = -Y(6,1) + BBC
     BBC=0.
     PT=-7(10,1)+ALP/57.6
     Y(2,1)=V1+CCS(PT1
     Y (4,1) = V1 = S IN(PT)
     FS=0.
     ER=0.
     EP=0.
     WRITE(6,920)(Y(K,1), R=1,N)
     CC51=1.14
     V(1)=Y(1)1)
     CCNTINUE
     CALLMCCAMS(X6H, MPT, N, Y, YP, CER, IK)
     x=0.
     TIPEO.
     IF(CSPEEC.GT.1.)GOTU2
     IT=11+1
     DG101=1.14
     Y([,L)=V([)
     Y(10,1)=Y(10,1)-CTF+IT
     Y(5,1)=-Y(10(1)
     Y(5,1) =- Y(1061)
     IF(TZ.GT.0.)GOT012
     Y(5,1)=Y(6,1)
 12 CCATINUE
     v2=v1
     Y(2,1)=V2+CCS(Y-10,11)
     Y(4.1) = - V2 = 3 : N(Y(1C, 1))
     EP=J.
```

```
FS=O.
      ER = 0.
       TIPSO.
      WRITE(6,900) FPT, H. TEN, AR, OVI. VI, OTH, ALP, RANGE, LOS, GBIAS
      *.VLAZRP,XLASR
hRITE(6,9201(Y(X,1),K=1,N)
1F(IC-IT)15,15,6
      CCATINUE
  15
 920
      FCRFAT(1P6E12.4)
  20
     STCF
       EAC
      SUBROUTINEDER(X,N,Y,YP,H,LZ,LY)
CIPENSICNY(14,6),YP(14,6)
       CCFFCN/VAR/TEN, AR, TIM, THF, TTK, TACC, GBIAS
      *,YFL,VLAZRP.XLASR
*,EP,FS,ER,TZ
REALMAS,IXX,IYY,IZZ,MAC
       PLC GUICANCE
YF(5,1)=-(EP+FS)/A4
C
       PURSUIT GUICANCE
       YP (5.1) 4-EP
       SICE WINCER GUIDANCE
       A8=20. . 6.28318
      1+YP(10,1))+A8++2
       C2=10./PI
       C3=.001/PI
       C4=1./PI
       P1=57.295776
       YP(5.1) -- EP (C2 - (ER-FS) + C3+FS
       YP(9:1)=0.
       YF(8,1)=-2. -A7 -A8 -Y(8,1)-A8 -+ 2 - Y(7,1)+C4 - (YP(5,1)
       RANGE=SCRT(Y(1,1)++2+Y(3,1)++2)
       TC=.25
       TF=1.3
       TZ=0.
       TR=.8
       RF=.072/32.2
       V1=(Y(2,1)++2+Y(4,1)++2)++.5
       C=.5 . RH . V1 . V1
       AL=(Y(2,1)+SIN(Y(10,1))+Y(4,1)+COS(Y(10,1)))/(Y(2,1)+COS(Y(10,1))
      1)-Y(4.11*SIN(Y(10,1)))
       IFIAL.EC.O. IGOTC42
       BL = ABS (AL)
       AL=FL/EL +ATAN(BL)
  42 CCATINUE
       C=.416
       XC=8.4.C
       ES=.136
       TTCT=7500.0.8+3750.0(TF-TR)
       Y(7,1)=Y(7.1)+GBIAS#1.5/57.6
       P1=12./57.6
       PL=24./57.6
       PP=#85(Y(7,1))
       1F(FP-P1)4,4+3
      Y(7,1)=Y(7,1)/PP+P1
      CONTINUE
       IF(X.GT.TR)GCT030
       TH=7500.
       TTC=7500.-X
       TICATTC/TTOT
       GCTC33
  30 1F(x-TF131,31,32
```

. Lagrage EE (A)

```
32
  TH=0.
    TTC=1.
    GCTC33
  Th=7500. • (TF-X)/(TF-TR)
31
    TTC=(TTCT-TF+(TF-X)+.5)/TTQT
33 TYC-1.-TYO
    XCG=(8.75+(10.6-8.75)+TTG)+0
    MAS=(3.48+(4.21-3.48)+TTG]
    1xx=(.0586+(.0914-.0686)+TTU)
    1YY=25.04+(29.56-25.04)+TTO
    TZZ=IYY
    MAC=V1/1150.
    IF (MAC.GE.2.)MAC=2.
    IF(FAC.G1..75)GCTO10
    CA=.4
    GCTC12
10 IF (MAC.GT.1.2) GUTO11
    CA=(FAC-.561+.6/.24
    GCTC12
11 CA=I.44-PAC+.22/2.8
    1F (TH. EC. 0.) GOTO13
    CA=.93 • CA
   CCNTINUE
    IF (MAC.GT .. 92) GOTO 16
    DC A=(.25 *MAC **3+.63) *(ABS(Y(7,1)*2.88)) 4*2.2
    GCTC17
  CCA=(-(MAC-2.8)**3*.0375+(MAC-2.8)*.12+.4)*(AB5(Y(7,1))*2.88)**
  12.1
17 CCNTINUE
    CNC=3.9-CCS MAC=3.14159/2.81+.7
    TF (FAC.GT..75) GOTO 18
    CN4415.8
    GCTC21
  IF (MAC.GT.1.)GOTO19
    CNA=15.8+9.2/.36*(MAC-.75)
    GC TC21
   IF (#AC.GT.1.5) GOTO20
    CN 4421.3
    GCTC21
   CNA=(MAC-2.8)++2+.71+20.1
    IF (MAC.GT.1.)GOT023
    CMC=(MAC) **315 *10.3+4.3
    GCTC24
23 CMC=EXP(-MAC+1.)+14.6+(MAC-1.)+4./1.8
    XCP=(-(MAC-.6) -- 2 - .632+14.02+(MAC-.6) -- 4 -. 1021 -- 416
    1F ( MAC. GT.1.4 ) GCT026
    CMT-MAC 4 # 2 # 850 . + 3700 .
    GC TG28
26 CMTREXP(-MAC+1.4)+56CO.+(MAC-1.4)+2150.
    CENTINUE
    F1=-(C4+2.*(CA+ABS(Y(7,1)))+Q+ES+TH
    F3 = - (CN# - AL +CNC +Y(7, 1) 1+Q+E3+TF+SIN(TEN)
    A1 = 10.
    A2 = .08
    A3=10.
    A4=4.
    A5=2-/57.6
    46 . TC
    A7 = .5
    A8 = 80.
    A8 = 20.
```

angelya, a servencya, p<del>arte letter parte lette letter l</del>

A9=1.

```
B1 = - (1 . +2 . + A7 - A8 - A2)/A2
    B2=-(A8 .. 2 . A2+2 . . A7 . A8)/A2
    63=-A8 + +2/A2
    84=-A8 . . 2 . A 3 . A9
    R5=P4/42
    86=84 e # 1
    YP(1.1)=Y(2.1)
    YP(3,1)=Y(4,1)
    YP17.11aY(8,11
    YP(8.1)=Y(9.1)
    YF(10,1)=Y(11,1)
    22=22-.1
    22=1[M+.1-X
    IF (22.61.0. ) GOTO7
    TIPEX
    ZK3=[[].+200./RANGE]+6.]
    IF(ZK3.GT.15.)GGT07
    EP=Y(10.1)
    SETRO.
    . 0=444
    CALL GAUSSISZT, AAA, AAV, X)
    IF (YFL.GT.VLAZRPIGCTO7
    SST4C.
    SSX=XLASR+SIN(Y(6,1))/RANGE
    CALL GAUSSISEX, SST. SSXV. X1
    FS=-SSXV/RANGE+Y(5,1)
    ER=Y(6,1)
    CENTINUE
    IF(TZ-X)80,81,81
81 FS=-EP
    YP(5.1)=0.
    GCTC85
    YP(5,1)4-(EP+FS)/A4
80
    CENTINUE
    YP(6,1)=1./(Y(1,1)++2+Y(3,1)++2)+(Y(1,1)+Y(4,1)-Y(3,1)
   1 - 7 (2 - 1 ) }
    YP(9,1) +81 + Y(9,1) +82 = Y(8,1) +83 + Y(7,1) +85 + (ER-FS) +86 + ( YP(5,1))
    YP(11,11*-CHT+Y(11,11*(RH+V1/4.)*ES+D+2/1YY+Q*ES+D/1YY+(-CNA+(XCP
   1-xCG) + AL+CNC + (XCG-XC)+Y(7,1))+TH+AR/IYY
    IF(ABS(YP(9.1)).GT. 1000.)YP(9,1)=SIGN( 1000.,YP(9,1))
    YP(2,1)=(F1+COS(Y(10,1))+F3+S1N(Y(10,1)))/MAS
    YP(4,1)=(-F1+SIN(Y(10,1))+F3=COS(Y(10,1)))/MAS+32.2
    AA=13.
    YP(12,1)=-V1-COS(Y(13,1)-Y(14,1))
YP(13,1)=-V1-SIN(Y(13,1)-Y(14,1))/Y(12,1)
    YP(14,1)=AA+YP(13,1)
    IF(X-TC)40,50,50
    YP(9,1)40.
    YP(8-1)40.
    YP(7.1)=0.
    YF(14,1)=0.
    YP(13,1)#0.
    YP(12,11*0.
    GCTC70
    IF(X-TC-F)60,60,70
50
    Y(13,1)43.14159625/2.-Y(6,1)
     Y(14,1)=3.14159625/2.+Y(10,1)-AL
     Y(12.1)={Y(1;1)++2+Y(3,1)++2)++.5
     YP(12,1)=-V1=COS(Y(13,1)-Y(14,1))
     YP(13,1)=VL =S[N]Y(13,1)-Y(14,1)]/Y(12,1)
     YP(14.1)*AA*YP(13.1)
   CONTINUE
70
```

```
TACC=SCRT(YP(2,1)==24YP(4,1)==2)
  RETURN
  ENC
  SUBROUTINEMCCAMS(X++,MPT+N+L+F+DER+IK)
  CIMENSICAU(14,6),F(14,6)
  CCMMCN/VAR/TEN.AR.TIM, THF. TTK. TACC.GBLAS
 .,YFL.VLAZRP.XLASR
 ·,EF,FS,ER,TZ
  CATA PREC1, PREC2, PREC3, PREC4

/55.0, -59.0, 37.0, -9.0/

. CCRR1, CORR2, CORR3, CORR4

/9.0, 19:0, -5.0, 1.0/

F24 # H / 24.0
                                                                                PDM00130
                                                                                MDM00140
                                                                                 P0H00150
                                                                                 FDMC0160
                                                                                 PDM00170
      P1 + PREC1 + H24
  P2 = PREC2 • H24
P3 = PREC3 • H24
      P4 = PREC4 + +24
C1 = CORR1 + H24
                                                                                 PDM00190
  C2 x CCRR2 • H24
C3 x CCRR3 • H24
      C4 = CORR4 . H24
                                                                                 MDM00210
  CATA ALPHAZ. ALPHA3
                                                                                PDM00249
      / . 4 . 45573725/
                                                                                 PDM00250
       "BETAZI, BETA31, BETA32, BETA41, BETA42, BETA43
                                                                                 PDM00260
       /.4, .29697761, .15875964, .2181004,-3.05096516, 3.83288476/
.OMEGA1, DMEGA2, DMEGA3, DMEGA4
                                                                                MDM00270
                                                                                PDM00280
       /-17476028,-.55148066, 1.2055356, .17118478/
                                                                                PDM00290
  CALLCER(X,N,U(1,1),F(1,1),F,1,1)
    IF (MPT .LE. 1 ) RETURN
                                                                                PDM00320
      AZ = ALPMAZ . F
  A3 = ALPHA3 + H
      821 = BETA21 . Y
  831 = 86TA31 + H
832 = 86TA32 + H
      841 . BETA41 . F
  842 = 8ETA42 . F
  843 = 86TA43 . F
      C1 3 OMEGA1 . F
  C2 = CMEGA2 + H
C3 = CMEGA3 + H
      C4 = OMEGA4 . F
                                                                                 ₩0₩00370
      LL = MINO (3,MPT-1)
                                                                                 PDM00380
  CC 10 K * 1.LL
                                                                                 *DM00390
  CC 1 [ = 1, N
                                                                                 PDM00410
       U(1,5) = U(1,K) + B21 + F(1,K)
                                                                                 MBM00420
1 CCNTINUE
                                                                                 MDM00430
                                                                                 PDM00440
  CALLCER(A,N,U(1,5),F(1,5),F,5,5)
  CC 2 I = 1.N
                                                                                 MDM00460
       U(1,5) = U(1,K) + 831 + F(1,K) + 832 + F(1,5)
                                                                                 MDM00470
2 CCNTINUE
                                                                                 M0M00480
       A = X + A3
                                                                                 PDM00490
  CALLCER(A.N.U(1.5).F(1.6).F.5.6)
  CC 3 I * 1.N
                                                                                 PDM00510
      U(1,5) = U(1,K) + 841 + F(1,K) + 842 + F(1,5) + 843 + F(1,6)
                                                                                FDM00520
3 CCNTINUE
                                                                                 P0P00530
      X = X + Y
                                                                                 PD#00540
  CALLDER(X,N,U(1,5),U(1,6),H,5,6)
  CC 4 I = 1.N
                                                                                 PDM00560
       U(I_1K+1) = U(I_1K) + O1 + F(I_1K) + O2 + F(I_15)
                                                                                 M0M00570
                            + G3 + F(1,6) + O4 + U(1,6).
                                                                                 P0P00580
4 CENTINUE
                                                                                 PDM00590
```

and single

```
LC=K+1
     CALLCER(X,N,U(1,K+1),F(1,K+1),F,LO,LO)
  10 CCNTINUE
                                                                       P0M00610
       IF (PFT .LT. 5) RETURN
                                                                       PDM00620
     K * 5
     KT=0
     JK=IK
     CC40LK=5; MPT
     CC 20 J * 1.N
         U(J_{+}K) + U(J_{+}K-1) + P1 + F(J_{+}K-1) + P2 + F(J_{+}K-2)
                                                                       P0200404
                           + P3 + F(J,K-3) + P4 + F(J,K-4)
                                                                       PDH00670
  20 CENTINUE
                                                                       F0H00680
     X = X + F
     CALLCER(X,N,U(1,K),F(1,K),F,K,K)
     DC 30 J + 1.N
                                                                       PDH00700
         PDM00710
                                                                       PDM00720
  30 CCNTINUE
                                                                        FDM00730
     CALLDER(X,N,U(1,K),F(1,K),F,K,X)
     1F (K-6)32,33,33
  32 K=6
     GCTC37
  33 OC341T=145
     DC34JT=1;N
     U(JT.IT) = U(JT, IT+1)
     F(JT:IT) = F(JT:IT <1)
  37 [F(JK-6)36,36,39
  42 JK=JK+1K
  36 WRITE(6,11)((U(JJ,JK),F(JJ,JK)),JJ=1,N)
     WRITE(6,11)X,TACC
     IF'(JK+IK=6)42,42,43
  43 JK=JK+IK
  39 JK=JK-1
     IF(U(3,51)40;40.12
  40 CCNTINUE
                                                                        PDM00750
  12 CENTINUE
     JK=JK-IK+1
     WR[TE(6,11)((U(JJ,JK).F(JJ,JK)),JJ=1,N)
     WRITE(6,11)X;TACC
  11 FCRFAT(1X,1P9E12.4)
                        RETURN
                                                                        FDF00760
                                                                        PDM00770
                        ENC
     SUBROUT INEGAUSS (S, AM, V, T)
     CCMMEN/VAR/TEN, AR, TIM, THF, TTK, TACC, GBIAS
     .,YFL,VLAZRP,XLASR
     ., EF, FS, ER, TZ
     S-THE RECUIRED STANDARD DEVIATION
     AM-IS THE RECUIRED MEAN V-VALUECE COMPUTED NORMALLY DISTRIBUTED RANDOM NUMBER
C
     IF(T.GT.0,)GOTO4
     IF([X)7.8.8
     IX = -IX
    IF ( IX. GT. 999
                     )GCTO3
   8
     IX=1X+2+1
     A=0.
     GCTC4
     1x=1x/10
     GCTC2
     CC501=1.12
      IF(1.GT.1) IX*IY
```

**1** 

```
J=IX-262147

1x=J.ANC.K

1Z=IX.AND.J

B=FLCAT(IZ)/3.4359739E10

YFL=8.AND.E

IX=IY

50 A=A4YFL

V=(Z-0.)+S+AN

RETURN

ENC

7

1.0000E+03 Z.0000E-02 0.0000E+00 0.0000E+00 0.0000E+00 5.0000E+02

Z.5000E+00 0.0000E+00 0.0000E+00 9.7500E+00 Z.5000E-01

Z.5000E+00 0.0000E+00 0.0000E+00
```

										•
	H+7326E-61 0.6 0.0	H.732/F-0; 0.0	73276-0 0 73296-0 5767E	6.735E-01 6.735E-01 6.622F 02 6.8374G-01	H.7351E-01 -9.2661E C1 6.7804E-01	6.73946-01 -6.46185 01 -6.72165-01	2.2.50(E-01) -2.2.51(D) -2.2.51(D)		10000000000000000000000000000000000000	0 1 6 6
	1.1 511E 03 0.0	1.14406 03	14 15 5 16 3 0 5 0 6 0 1 1 1 1 7 0 0 7 1 1 3 3 0	1.1913. 03 1.1913. 03 1.166.65 6.56465	1.21095 03 9.52935 00 -7.25155-03	1.22A7F 03 8.53310-01 47.4221F-03	2000 C 66 11/1 9 64 36F - 0		اع و د	0 = 30 0 0 0 0
	0.0 0.0 0.0	5.7336E 02 0.3 0.0	55 miles	6.0313E-01 6.5243E-02 -1000002-03	0,000 000 000 000 000 000 000 000 000 0	1.03 4616 93 8.53316-51 6.07456-01	-14567 -04486 -CAUSE	10-14:00	10-110-110-110-110-110-110-110-110-110-	10 - 3 × 0 × 0 · 0
0.0	9 9 9 7 7 * *	5.7338E 02 0.0 0.0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	8-2245E 62 -5-4957E 66 -1-1005E 63	3.1649E 62 -5.1418E 00 -1.229EE 03	80 300000000000000000000000000000000000	1 181	4.7.05.KF -4.7.05.KF -1.5.0.00 -1.5.00	7797E 0	60 Jest 6.15
4,7326=-01		-9.5165E 03 0.0 1.6300E 03	9.0 1.00.00E 03 1.00.00E 03 -2.42.4E 03 -7.59.00E 30	1.1977 03 -0.7573E 03 -5.77573E 03 1.18945 04	-9.6977. 03 -5.3413F 00 1.18016 04	-9.80 79E 63 -3.9512E 60 1.1697E 64	02E 03		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1.11531 0-
0.0 0.1401E 02	1117F	9.3275E 02 6.0 -9.4219E-02	.42(25 .43996-	9,11566-01 9,11566-02 -2,09,38-01 -1,15146-00	.0333C-	.4002E .0433E	8.2507E 02 -2.0135-01 1.1246E 00	09336-	6. 73 17 6 6. 73 17 6 6. 73 17 6	-5-6-198-01
S 5	0242E 0 3851U-3 3651E-0	4.7559E 02 5.1383F-03	5, 5163k 92 5, 6246f-33 -1,50,716-03 5,2716k 92	7.01076 02 7.14125-01	7.72826 02 7.8926-03 1.72996-01	3.416%c G2 0.0463%c03	03 0,032 to 02 01 0 02 03 1 0 03 02 03 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	7.4570E-03 7.4570E-03 -1.7310E-03	7. mark - 93	10-11170-1-
7.305 -0.1	3.0 3.0 3.02421 02 4.5)3751-01 -1.05518-01	1.4551E 03 4.7637E 02 5.6075E-01 -6.3554E-63	1.47515 03 5.31626 02 5.31746-61 -1.56626-02 1.437,10 03 6.27706 03	1.43516 63 7.5316 03 7.5316 03 7.5216-01	1.5coue 03 7.7cm2E 02 9.02942E-31	1.4974E 03 E.104E 02 9.5145E-01 -1.46647E-01	20-04-1-03-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-		• •	-1.231t-01
3000 33 4336-32 5006 63	~ -	0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.0	2 - 1 - 2 - 2 - 2 - 2 - 2 - 2 - 2 - 2 -	-4.75158-01 -5.57-10-02 -5.57-10-02 -6.60-03 -6.00-03 -6.00-03 -6.00-03 -6.00-03 -6.00-03 -6.00-03 -6.00-03 -6.	10 - 20 F 20 - 20 - 20 - 20 - 20 - 20 - 2	4.1.5012.02 4.1.506.01 4.1.506.03 4.1.606.03 4.1.606.03 4.1.606.03	10-130002-0	20 - 32 1 7 0 - 21	1 1 1 1	10+1010+8 20+1010+8 10+11010+8

1.1.10.00 -1.1.10.00 -1.10.00 -1.10.00 -1.10.00	0.73546-01 h.5447F 00 t. 37916-61	HC11E-0 0602E 0 3319F-0	5 E V 2 L	4, 84.3 of -61 3, 704.3F 01 6+2 34661	8.5542C-01 -3.6952L-01 6.1H85L-03	9.4708F -4.214CE 6.1036E	100 400 400 400 400 400 400 400 400 400	15.03.04 10.03.02.0 10.10.03.00	10-320426-6
9.3%42c C2 1.4279F G0 6.0055L-03	7 1515 62 2.53788 00 -6.1735E-03	5.0045E 1.1066E -5.6169E	, ,	-7-48546 0: 3-2242 00 -3-74946-01	1.2375E 01 1.2345E 00 -0.3961E-03	-7.6435E 2.473c -2.5523:	- 7. 72807 01 - 7. 72807 01	-2.23276 -7.23276 -7.27376 -1.51600	' '! '
10-00-00-00 1 00-00-22-0-1 00-00-22-0-1	2.5.1785. C3 2.5.1785. C3 1.6.04026. C3	1 !	1 - 1 94 1E 0 - 0 31 2 7 1 C	3 1.6 B51E 33 0 3.2242F 56 3 6.0240E-01	3 1.04400E 03 0 1.2365E 00 3 6.2211E-01	1.67392 2.4973E 6.0166E	3 1-0678c 03 0 3-927c 03 3 6-016-6-01 3 1-0615E 03	3 6.71845. 3 1.75548. 3 1.75548. 3 7.07076. 3 6.012842.	3 1.64-01; 03 0 1.64-02; 03 1 6-01; 34-31 3 1-64-29; 03
1.529/E 33 -4.5426E 00 -1.916CE 03	1 -4-4-106 00 1 -4-4-106 00	1.6760E 2	-4.1434E 0 -2.0604E 0 1.0302E 0 -3.9071F 0	1.6361E 0 -3.8482E 0 -2.0517E 0	1.0800E C - 3.0338E C -2.034E O	1.0737E 0 -3.4 CHAE 3 -2.0172E 0	1.4678E 0 -3.2033E 0 -2.0003E 0	1.0944E 0	1 1.00401E 0 0 -2.4276E 0 2 -1.49515E 0
	2 -3.0042E US 1 -4.4310E US 1 1.0380E 06	-3-93431. -4-2H72E 1-0727E	1.0562C 0 1.0562C 0 -11.5946E 0 -3.997E 0	-0.4314E 0 -3.6482E 0 1.3233E 0	2 -8,2967E 03 1 -3,5339E 00 2 1,0070E 04	-6.1625f. -J.4083E 9.9076E	-8.02986 -9.20356 -9.74699	2.597.62 9.597.62 -7.7523E -2.7058-	-7.6.136F -2.1.276E 9.27.25E -7.4988E
1 4.44214 02 1 -2.0133E-01 1 3.4401E-01	3-0027E 0 -2-0038E-0 3-3636E-0	1, 15476 -2, 03538 -3, 03318 -3, 21786	17.	-2.9055E 0 -2.0438-0 1.1304E-0	3 -2.7336 02 4 -2.73318-01 2 -6.33856-02	-2.67745 -2.0335- -1.75096-	77 7		-2.0438E-0 -2.043E-0 -2.0549E-0 -2.423E-0
10-18-50 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0 04779E 0 0 0477E 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1 -1-15551 33 1 1 -4-75974-03 -2 2 -6-92161-02 -3 2 1-15466 03 -3	i ' i'	1 1.1007E 03 1 7.6006-04 2 -0.5619E-02	2	1.1263E -2.1565c-	1 1.1047E 0.1 1 -3.6787E-0.3 2 -3.0155F-72 2 3 1.6839E 0.1	1.06356 	2 1.04.36E 0.3 1 -0.04.04 0.0 1 -0.06.00C-0.2 2 -0.06.00C-0.3
1.14636 63 9.88525-01 -1.67536-01	1.03224 1.17725 5.07025 -6.0316E		2,7954E-02 2,7954E-02 2,7954E-03 1,1964E-03 0,5401E-01	2,0347E 02 1,1597E 03 9,6313E-01	7. 3041F	2.7855E G2	,		
1.212.15.03 1.212.16.02 		20.000 00		1.28 CGE 09 1.28 C	20104644 20104644 20104644 20104644 20104644 20104644 20104644 20104644 20104644 20104644 20104644 20104644 20104644 2010464	-5-61726 03 -5-61726 03 -2-20505-02 -9-40611-91 -2-55525-55 1-50506 09	-5.5279E 03 2.3729E 03 -9.8737E 03 -2.5666E 62 1.5560E 06 -5.4437E 03	2.5725-02 -9.9495L-01 -9.9495L-02 -1.4493CE -5.3493C-03 -5.3493C-03 -5.5725-02	

3-14-01E-02 9-75-01E-02 9-75-01E-01 5-13-02E-01	01 -1-90286-01 02 3-1-615-02 01 -1-7115E-01 03 -1-7115E-01	2.0438E-01 -5.0068E-03 -2.0064E-01 -2.0064E-01 -5.0464E-01	1,30,45E 04 1,3777E 04 1,3777E 04 1,3740E 03	1.00045 04 1.00004E 04 1.00004E 04	6.0021E-01	8.3720E 00 3.0 3.0 2.2859E 01 1.3594F 31	6.0021f-01	
5.5196E 01 8.31725 02 7.1921E-01	0.0172E 02 -1.9732L-01	-2. C. 0. 3. C. 0	20 300 00 0 1 0 3 0 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0 0 1 0	1.0230E 0	2 - 2	0016E	4 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 +	
20 37 10 05 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	2000 C	2 CH 31 - 01 -	71 24 24 24 24 24 24 24 24 24 24 24 24 24	1.0 159E 0	000	-8.8458F 01	10000000000000000000000000000000000000	
4.00 fnt 01 7.00 34E 02 6.02 04E 01 7.00 24E 02	7.58530 02	-1. \$4426 2.09.136 -5. C709E	-6.4340E 02 1.5547E 01	C 348401 C 348401 C 348401 C 348401	10 28496 03 10 76356 01 50 62 18 - 61	-8.6387c 01	9.54.32F- -2.50.9EE -2.50.9EE	
6.4543E 01 7.9573E 02 6.5773c-91 2.9417E-52	7.96446 (2 -3.3176 - 01 2.90179 - 62	2.04331.01 2.04331.01 2.4.932E-03	-5-6305c 02 3-8026f 01 8-5967c 02		500	-8-42795 UB 2-60595 GB 0-0	0.5322-01 8.4243F 01 6.0021E-01	
6.04 4E 02 6.23 J.E-01 2.9031E-02	02 7.954ME 02 01 -4.1070E-01 02 2.4031E-02	-1.6516F 01 2.0431E-01 2.4.7479E-03	1.02.40E 02	4-4536E 02 1-9589F 01 -1-2742E 03	0.0021E-01	-A-24-MC CI 1-4173E GI	9+5216E-01 1+375+E-03 6+6021E-01	
8.4501£ 01 7.4401£ 02 5.9134E-01 4.9763E-02	01 02 704615 02 01 -5.22211-61 02 2.86035-62	2.0433E-01 -4.4433E-01	\$ 1816.65 \$ 1816.65 \$ 1816.68	7-3-3-3-5-0-2-2-3-3-0-1 -1-2-6-3-6-0-3-	2.1796 01 6.072101	-0.0384( 0) 2.17086 01 0.0	9.509EE-01 -4.19945 02 6.1071F-01	
4,2587E 91 7,427 :E 52 5,434,6-01 2,431 :E-02	21 22 7.925,40 62 - 31 7.67,8547,761 32 2.8313102 -	1. 75556 01 2. ch 3.50-01	2-1019 1F 02 2-101F 01 5-5-101F 01	04H740F 02 240644E 01 -142623F 03	4.45466 02 4.52726 01 6.00216-01	-7.97855 FL 4.42725 31	9.497 FE-01 -3.74000 02 -5.0021E-01	
7.4114E 02 4.7427E-01 5.7457E-01	02 7.5116F 02 01 -4.3765L-01 02 7.765R-02	2. CH38F-01	-2.44.5HE 02 2.74.24L 01 4.5321f 02	9.7622c 02 2.7429E 01	9.70220 32 6.82300 01 6.00210-01	-7.7051E 01 6.5230E 01	9.4859F-61 8-4736F-02 6-6321E-11	
7.8×53F 63 F.4442E 62 3.44×34E-61 2.75°2E-02	02 7-792L 02 02 -1-1447-00 02 2-75471-02	-1.6451E 0; 2.0838-C; -4.5209E-03	-1.08726 02 3.00676 01 3.02911_02	4.70126 02 3.20676 01 -1.2519E 03	9+70125 02 2+73565 01 6+70216-01	7.537 <u>2</u> 01 2.71360 0.0	9.47376-01 -7.9854E F2 0.03216-01	
7. 3.3.9.0.02 7. 3.4.4.0.02 7. 3.4.0.02 7.	01 7-984 16 05 01 -2-31511 00 02 2-72425-03	-1,6470F 61 7,0913E-01 -4,1710L-03	-9+13531 01 -9+13531 01 	4.0415E 07 1.7267E 01 -1.2359E 03	9-5-61-5: 02 577-3: 01 6-00215-01	-7.3753E C! 6.4779F O. 0.0	9-461 3F-01 -1-3576 63 6-0216-01	
7.05.396-07	02 7.8717F 02	-1.61526 01 2.0813E-01	-1.4455C 01	10 3608 W.*	1.00335 02	1.5933C 02	0.148AF-01 -5:1427C 07	

9.0252E 01 3.255E 01 1.0778E 02 1.359E 02 1.4778E 02 1.359E 02 1.4178E 02 1.359E 03 1.0778E 02 1.459E 02 1.459E 02 1.450E 03 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0	16-14E-01	2.6400F-52	20-10004-2	4.13405-03	1153625 62	-1.2402F 03	10-7120074	o.0	6. 30216-01	1
1,75   1,	o 2	7.4701F 02	/.d .011. 32		-4.0/0:0	4.5759E 0	7 . A. 02	7.11935		
2. A JUNE CO. 3.		1.75261 52	- 3.4.44	-	5.0252F	S.J.25.E. G	3	310.60	-1.1395E 0	
1.000000 0.0 1.0000000 0.0 0.0 0.0 0.0 0	_	2.53516-02	2.005%	;	1.41.226.	-1.23956 0	,	2.0	6. C021E-01	
1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1		1								
1,000 = 0, 1,000 = 0,	•	30000			0.0	0.0	;			
1.1000 0 1 1000 0 1 1100 0 1 1 1000 0 1 1000 0 1 1 1000 0 1 1 1000 0 1 1 1000 0 1 1 1000 0 1 1 1000 0 1 1000 0 1 1 1000 0		10-200				-				
1.000E 20 1.000E 20 1.000E 20 0.00 0.00 0.00 0.00 0.00 0.00 0	!	30 ap 05	Č	-74	6576-0	-370:00				
1-1000	، ر.	0.0		••	0.0		:			
1.0000E 0.0 1.0000		0.5	50-3000		0.0	0-0				
1.00006 03  1.0000		1	10101			•	•	•		
1.0000		9 9		14516 02	10-39	9.6007E-01				
1.00004-0. 1.00004-0. 0. 1.0004-0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0	1			7 326E -01		1.0000E 03				
## 1921   1.   1.   1.   1.   1.   1.   1.	J	0.0								
11-31-004_C 0 1 1-13-004_C 0 2 1-10-04 C 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	٠,	4.1521E 02		. 1524E 0	. 97.262 3	954E	324E	o Y		The state of the s
143704E-01   113004E-03   11804E-03   118004E-03   0.0   0		9.603225-01		0.0		0.0	0.0	0.0	0.0	
1.63 46 6 03  5.53 73 6 0 5 5 5 5 5 5 5 6 5 6 0 5 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1.33005-03		-3. #221E	0	0.0	o•0	0.0	0.0	
1.43 94 6 0 3 6 0	-									
5-50726-02 5-50956-02 1-105016-0390776-03 0-0 0-0 0-0 0-0 0-0 0-0 0-0 0-0 0-0	7					,	,			
0.00 722-01 515000-03 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0		5.3.795E CC		1.15636 C	٥.	17:E 0	1715 0	13 Q11	8.73275-7	
1.89 yr 03 6.00 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0		7.50 72E- 01		0.0		0.0	0.0	c	ن. د	
1.83.27£ 03 6.020.02 0.000.02 2 1.174*1 03 -9.8745E 93 7.2034E 92 7.2034E 02 1.1154*1 03 6.020.02 0.000.03 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.		6.5737E-53		-4. 40 / E	c	0.0	?•0	0.0	٠ <b>٠</b> ٥	
6.62606 67 0.02706 52 1.1744 63 90.8755 53 7.2034 6 52 7.2034 6 02 1.1360 6 03 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0		1000000								
1.8532E C3	1	1000	- 1		- 1	1	١,	1		
1.85 316 C3		5.5120F=01				1	7		26.00	
1.85 31E C 3  6.996.2E 2 2 3.6002. 22 1.1000. 01 -9.513E 03 -2.552E 00 -2.552E 00 -3.137. 01 -6.176. 11  -3.422E - 02 -3.422E - 02 -4.505. 02 -2.532E 03 -2.552E 03 -2.553E 03 -		1.08816-03	-	0-36.200-1-	400					
1.85.32E C.3								;	•	
9.6176E-31 7.5631E-03 -4.5501E-03 -2.5171E 03 -2.5721E 03 -3.1745E 01 -2.1745E 03 -2.5721E 03 -3.1745E 01 -2.1745E 03 -2.5721E	. 5	O							•	
4-6176-01   7-54312-03   -4-4505E-04   -2-5121E 03   -2-56121E 00   -3-13-2E 01   -7-7190E 04   -1-0635E 03   -5-727E-02   -4-5401E-03   1-1001E 04   -1-0635E 03   -5-727E-03   -7-7190E 03   -1-0635E 03   -5-727E-03   -7-7190E 03   -1-0635E 03   -5-727E-03   -7-7190E 03   -1-0635E 03   -1-07190E 03   -1		6.9062E 32		10465 0	-9.6119E 33	Ņ	5		A. 737 OE - 3	
-348275-02 -348276-02 -4-57016-01 1,19016 04 -1,05356 C3 6,0036-01 -7,2756-13 1.455826 03 7.89216 62 7.68216 62 1,12506 61 -0,73986 03 3,57346 02 4,5734; 02 1,67725 73 7.89216 62 7.68216 62 1,12506 61 -0,73986 03 1,07641 03 1,07646 03 1,07746	Į	9.61 74E-31	i		-2.532;E 03	3	5		1.6:776 0	
1.40542E 03 7.4931F G2 7.48421E G2 1.1250E 01 -9.7199E 03 9.5734E 02 9.5734E 02 1.47734E 03 1.4774E 03 1.47734E 03		3.42275-02			1.19616 04	Ü	-		0-30554.0	
1.45582E 03  1.45582E 03  2.45247E 02  2.45247E 02  2.45247E 03  2.45247E 02  2.45247E 03  2.452							,			***************************************
7.89216 G2 7.8821E G2 1.1250E G1 -0.7199E 03 9.5734E G2 9.57889 G2 1.67775 53 -0.6249E-01 -1.5774E G3 -1.67774E G3 -1.6777	5									
9.6249E-01 H.JENNE-03 -22.003JG-31 -0.0004E-06 -1.2370G-03 G-1.4074C-03 -1.4174G-03 J-1.4074C-04 -1.4074C-03 G-1.4074C-04 -1.4074C-04 -1.4074C-05 G-1.4074C-05 G-	50			-	.0.7398E 0	0	40 - 484 - 0V		0-141-7-0	
-1.301ce-01 -1.301cf-01 -1.3047E 00 1.1908F 04 -1.2370E 03 0.784201 -7.41702_03  1.8520E 03  8.7641E 02 9.7641E 02 1.00404E 03 1.0764F 03 1.0764F 03 1.0 (1) (3)  9.03042_01 9.6154E-03 -2.0043f-01 -5.4950E 00 -5.4850, 00 0.7.495E 00 0.7.770E  1.8950E-01 -1.6450E-01 -2.0043f-01 -5.4950E 00 -5.4850, 00 0.7.495E 00 0.7.770E  1.8950E-01 -1.6450E-01 -2.0043f-01 -6.4950E 03 1.1705E 03 0.7.770E  1.8950E-01 9.1217E-03 -2.0043f-03 1.0470 03 1.1705E 03 0.7.770E  1.8950E-01 9.1217E-03 -2.0043f-03 1.1647E 03 1.1705E 03 0.7.770E  1.89645E-01 9.0250L-03 -2.0043f-03 1.1704E 03 1.324E 04 1.4245. 03 1.5870E 03 0.7746  1.89646E 03 1.0043f, 03 1.0170E 03 -9.464E 03 1.324E 04 1.4245. 03 1.5870E 03 0.7746  1.89646E 03 1.0043f, 03 1.0170E 03 -9.464E 03 1.324E 04 1.4245. 03 1.5870E 03 0.7746  1.89646E 03 1.0043f, 03 1.0170E 03 -9.464E 03 1.4240E 03 1.0440 02 1.4740. 03 1.4240. 0		9.6240F-01		10-11100-2-	0 30000-4-	20 12 0000-4-	( ) \ \ \ ( \ \ \ \ \ \ \ \ \ \ \ \ \ \			
1.8520c 03 4.7631c 03 4.7631c 03 4.7631c 03 4.7631c 03 1.6050c 03 4.7631c 03 1.6050c 03 1.6050	!	10 3010E-01	10.161-01-	-1-3047F CO	144461	2000				
1.8520c 03 4.7541E 02 4.7541E 02 4.7541E 02 4.7541E 02 4.7541E 03 1.07641 03 1.07642 03 1.07642 03 1.07642 03 1.07642 03 1.07742 03										
## 7641E C2 ## 7641E C2 ## 04000 03 ## 03 ## 04 ## 05 ## 04 ## 05 ## 04 ## 05 ## 04 ## 05 ## 04 ## 05 ## 04 ## 05 ## 04 ## 05 ## 04 ## 05 ## 04 ## 05	-									• • • • • • • • • • • • • • • • • • • •
9.0.30295-01 -1.0.0.502-03 -2.0.0.316-01 -5.30500 00 -5.30500, 00 03.7090 00 04.7700 00	70			1.00001		0		31.00	11.7.4.45	
1.4573E 03 9-01-02-02-01-01-02-01-01-02-01-01-02-01-01-01-01-01-01-01-01-01-01-01-01-01-		9.03001		-2.04336		•			•	
1.45736 03 9-01056 02 9-01056 02 9-01056 02 9-01056 02 9-01056 03 1-1105776 03 1-110576 03		1.0950E-01	- 1	200,000		C		B. 14 02: -		
9-010-26 02 G-6-10-02 1-0-03-12-03-13-03-13-13-03-13-13-03-13-13-03-13-13-03-13-13-03-13-13-03-13-13-03-13-13-03-13-13-03-13-13-13-03-13-13-03-13-13-03-13-13-03-13-13-03-13-13-03-13-13-03-13-13-13-03-13-13-13-03-13-13-13-13-13-13-13-13-13-13-13-13-13	3 :									
1.9547E 63 1.9547E 63 1.95477E 63 1.9547E 63 1.954			304.4.5	10.40.1	.142	33			, ,	
1.96476   1.0437001   1.61031 00   1.15476 04   1.07751 03   6.07176-01   1.158106 03   1.04706   1.04	5	9-5 10.26-01	10.10.10	- 1 1 1 1 1 1 1	1000	1000			1 U C C C C C C C C C C C C C C C C C C	
1.0047F   G		10 121 121 101	•	1000			10 - 10 - 10 - 1		10.01	
1.8647F C J 1.9479E C J 1.0479E C J 1.047						0.00	10.11.000	200	1.00	
1.04/9E 03 1.03-33% 03 1.0174E 03 -9.4064E 03 1.3234E 04 1.32332 03 1.55846E 03 6.6454E-01 9.02554E-03 -2.5833E-03 -4.7481E 00 1.6744L 00 1.674	15	1.9647F CJ	i					1		
7.04546-01 9.02502-03-220138-01 1.15144 00 4.77018 00 1.67444 02 1.67444 02 1.57444 03 1.579156-02 -3.79156-02 9.51336-01 1.15144 03 1.67444 02 1.57444 03 1.579156-03 9.51336-03 1.579156 03 1.579156 03 1.57915	3	1.04.398 63	1.00-001	1 . C1 775			1.121.1		4-7463E-0	
-3.7915E-02 -3.7815E-07 0.5130E-01 1.151 E 34 -1.0450E 32 5.05045E-01 -0.35E1G-03 1.48049E 03 1.1230E 03 1.5575E 03 1.48040E 03 1.48050E 03 1.5575E 03 1.48040E 03 1.5575E 03 1.	-		9.07500	- 7. 111.						* · · · · · · · · · · · · · · · · · · ·
1.46494E 03		3.79155-02	-3-7815F-0			30000	30 355 00 7		1027101	
1.86.94E 03 1.124.0E 03 1.1224.0E 03 1.670.0E 03 -24.57.55.E 03 1.444.0E 03 1.444.0E 03 1.577.E 03 9.40.55.E 03 0.40.0E 0.0 -24.0B.3.E 01 0.40.90.E 06 0.40.90.E 03 1.572.E 00 0.40.90.E 02 -14.04.0E 02 -14.04.0E 03 0.40.0E 03 0.40.0	•	; ;		•		30 % 64			37050.0	
1-12446 01 11-12446 01 1-20105 01 -0-10-10-10-10-10-10-10-10-10-10-10-10-1	=	1.86996 03								
9.0525f-01 0.000xE-03 -2.000xE-01 -2.000x 00 -2.000x0 01 1.00x0 00	ļ	1.12446 03	1	1.650.45		0 7369 001	30.44.1	. / 6	i	
#1+8880E-02   1+4020E-02   F0-0063E-01   1-1147E 04   1-14820E 05   640572E-01   10-14820E		9-55256-01		-2.60935-		-4.69961 0	1.0 6.6 4	5000		
		1 . 8620E-02	•	٤	1.13778 04			•		

APPENDIX II
AERODYNAMIC CURVES

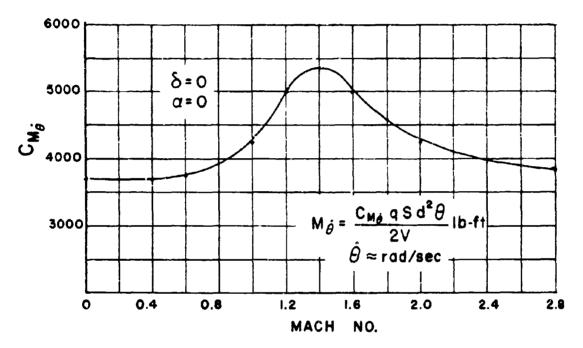


Figure II-1. Aero Pitch Damping Curve

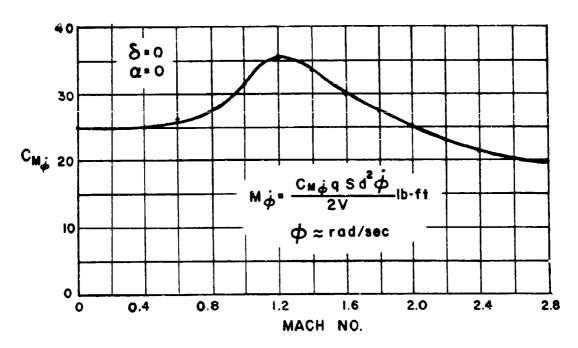


Figure II-2. Aero Roll Damping Curve

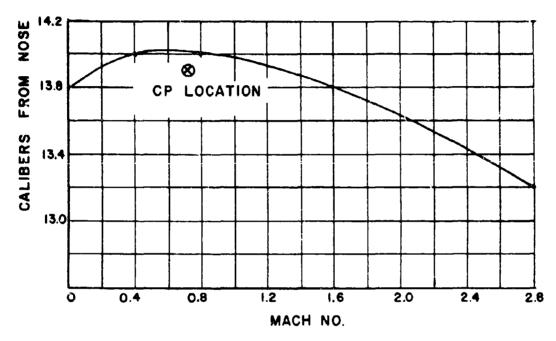


Figure II-3. Center of Pressure Location

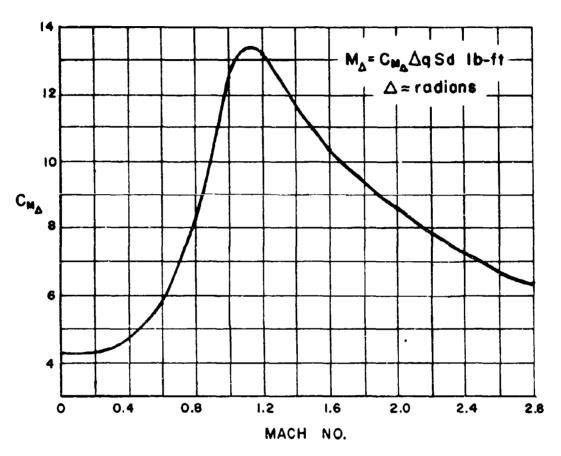


Figure II-4. Tail Misalignment Coefficient

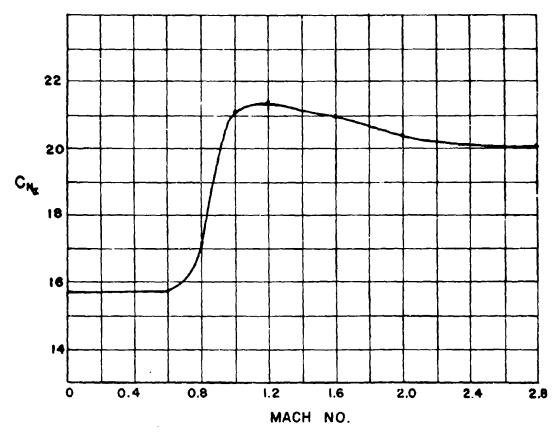


Figure II-5. Body Normal Force

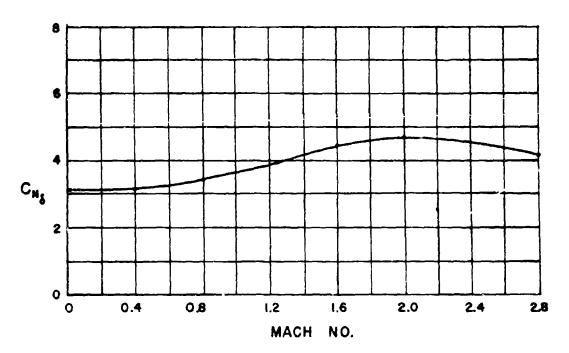


Figure II-6. Control Vane Normal Force

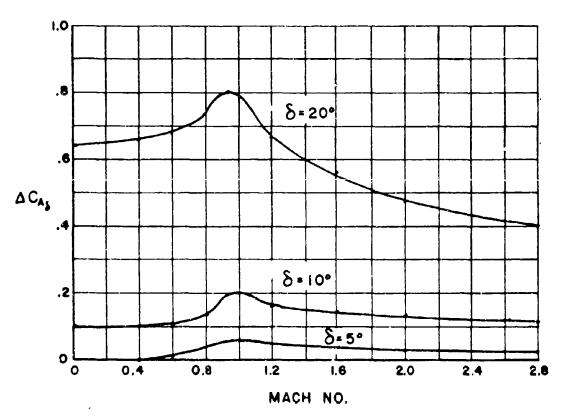


Figure II-7. Induced Drag

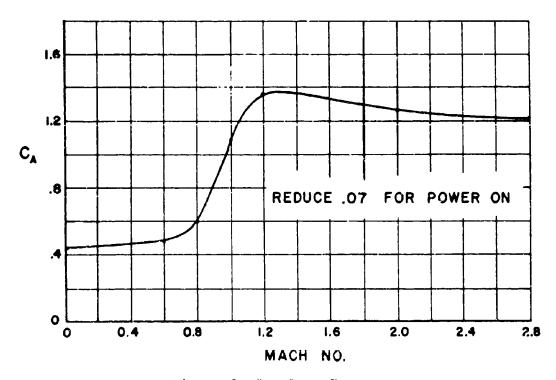


Figure II-8. Drag Force

#### REFERENCES

- Tokahashi, Y., Robins, M. J., Auslander, D. M., Control, Addison-Wesley Publishing Co., 1st Ed. 1970.
- Hsu, J. C., Meyer, A. U., Modern Control Principles and Applications, McGraw-Hill Book Co., 1st Ed. 1968.
- Saucedo, R., Schiring, E. E., Introduction to Continuous and Digital Control Systems, Macmillan Co., 1st Ed. 1968.

UNCLASSIFIED ecunty Classification DOCUMENT CONTROL DATA - R & D classification of title, body of obstruct and indexing annotation must be entered when the overall report to classified ZA. REPORT SECURITY CLASMFICATION UNCLASSIFIED Department of Mechanical Engineering University of Florida Gainesville, Florida CLOSE AIR SUPPORT MISSILE GUIDANCE AND CONTROL STUDY. olume II. Three-Degree-of-Freedom Simulation Mahig 16. NO OF REFS FØ8635-71-C-ØØ73 Work Unit No. Distribution limited to U. S. Government report documents the close his suppos control study; distribution limitation applied December 1971. Other requests for this document must be referred to the Air

This report describes in detail a three-degree-of-freedom program which can be used to determine the trajectory and miss distance of a guided missile system. The options for the program are such as to permit variation of the aerodynamics, seeker, autopilot, actuator, and missile motor performance for the purpose of accurately simulating a given missile design and evaluating the effects of any changes in system parameters. Sufficient detail has been included in the text to minimize the effort needed to update or modify the program presented.

Force Armament Laboratory (DLWG), Eglin Air Force Base, Florida

12 SPONSORING MILITARY ACTIVITY

Air Force Armament Laboratory Air Force Systems Command

Eglin Air Force Base, Florida 325 2

SUBSTARY NOTES

1 ARSTRACI

Available in CDC

UNCLASSIFIED

407260

Security Classification

UNCLASSIFIED

4	LIN	. A	LINK		LINKC	
KEY WORDS	ROLE	7.0	ROLE	W T	ROLE	w Y
Guided Missile	[					
Missile Simulation System						
Missile Simulation System Three-Degree-of-Freedom Simulation	1					
					i	
	ļ				}	
					ļ :	
	]					
						}
	l			l		
					(	
	j					
	l					
	[				[ [	
	}		1	ŀ		1
		Ì		İ		
	}	j	ļ		Ì	ļ
	1	]			,	
	1	1				
	1		ļ	}		; j
		<u> </u>				
	}	}	İ	İ		
	İ	1				
		1	ł	ļ	}	İ
			1	Ì	ì	
	}			Ì	Ì	Ì
		1	ł	}	1	
				1	}	
		i .	1	ļ		
			Į		1	
		ĺ	1		ľ	[
	}	1	}	ļ	}	
		]	1	1		}
			1	1		i
				1	}	1
	ļ			1		
		1	1	1	ł	{
	]		}	j	}	]
	1			1	1	}
		}			1	i
		1		1	1	
	}	}	1	1		1

Security Classification